

# Following Lenny's Lead

John Preskill  
DanLennyFest  
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## Hamiltonian formulation of Wilson's lattice gauge theories

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(Received 9 July 1974)

Wilson's lattice gauge model is presented as a canonical Hamiltonian theory. The structure of the model is reduced to the interactions of an infinite collection of coupled rigid rotators. The gauge-invariant configuration space consists of a collection of strings with quarks at their ends. The strings are lines of non-Abelian electric flux. In the strong-coupling limit the dynamics is best described in terms of these strings. Quark confinement is a result of the inability to break a string without producing a pair.

Loeb Lectures at Harvard 1977  
"Coarse-Grained Quantum Field Theory"

# Provably accurate simulation of gauge theories and bosonic systems

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Quantum many-body systems involving bosonic modes or gauge fields have infinite-dimensional local Hilbert spaces which must be truncated to perform simulations of real-time dynamics on classical or quantum computers. To analyze errors resulting from truncation, we develop methods for bounding the rate of growth of local quantum numbers such as the occupation number of a mode at a lattice site, or the electric field at a lattice link. Our approach applies to various models of bosons interacting with spins or fermions such as the Hubbard-Holstein, Fröhlich, and Dicke models, and also to both abelian and non-abelian gauge theories. We show that if states in these models are truncated by imposing an upper limit  $\Lambda$  on each local quantum number, and if the initial state has low local quantum numbers, then a truncation error no worse than  $\epsilon$  can be achieved by choosing  $\Lambda$  to increase polylogarithmically with  $\epsilon^{-1}$ , an exponential im-

the gate complexity depends almost linearly on spacetime volume in the former case, and almost quadratically on time in the latter case. We establish a lower bound showing that there are systems involving bosons for which this quadratic scaling with time cannot be improved. By applying our results on the truncation error in time evolution, we also prove that spectrally isolated energy eigenstates can be approximated with error at most  $\epsilon$  by truncating local quantum numbers at  $\Lambda = \text{polylog}(\epsilon^{-1})$ .

## 1 Introduction

Model physical systems are often formulated on spatial lattices, where the local Hilbert space residing on each site or link of the lattice is infinite dimensional. Examples include condensed-matter systems with bosonic degrees of freedom [21, 27, 43, 51, 52, 62, 64, 67, 76], lattice gauge

## Lattice fermions

Leonard Susskind\*

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*and Belfer Graduate School of Science, Yeshiva University, New York, New York 10033 †*

(Received 9 February 1976)

The problem of formulating the field theory of Dirac particles on a spatial lattice is reviewed. In one dimension we construct free massless Dirac fields and Thirring fields and show their equivalence to the  $X$ - $Y$  and asymmetric Heisenberg antiferromagnetic chains. In three dimensions we find that the simplest construction describes an isodoublet of massless Dirac fields. We discuss the incorporation of gauge degrees of freedom and illustrate how chiral symmetry is spontaneously broken by the interaction of gauge and fermion fields.

## CHIRAL GAUGE THEORIES ON THE LATTICE\*

Estia EICHTEN

*Fermilab,\*\* P.O. Box 500, IL 60510, USA*

John PRESKILL<sup>1</sup>

*California Institute of Technology, Pasadena, CA 91125, USA*

Received 5 November 1985

We propose a method for constructing lattice gauge theories in which fermions transform as a complex representation of the gauge group.

**Baryon number of the universe****Savas Dimopoulos\****Enrico Fermi Institute, University of Chicago, Chicago, Illinois 60637***Leonard Susskind***Stanford Linear Accelerator Center, Stanford University, Stanford, California 94305*

(Received 9 June 1978)

We consider the possibility that the observed particle-antiparticle imbalance in the universe is due to baryon-number,  $C$ , and  $CP$  nonconservation. We make general observations and describe a framework for making quantitative estimates.

**Cosmological Production of Superheavy Magnetic Monopoles****John P. Preskill***Lyman Laboratory of Physics, Harvard University, Cambridge, Massachusetts 02138*

(Received 21 June 1979)

Grand unified models of elementary particle interactions contain stable superheavy magnetic monopoles. The density of such monopoles in the early universe is estimated to be unacceptably large. Cosmological monopole production may be suppressed if the phase transition at the grand unification mass scale is strongly first order.

## Dynamics of spontaneous symmetry breaking in the Weinberg-Salam theory

Leonard Susskind\*

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(Received 5 July 1978)

We argue that the existence of fundamental scalar fields constitutes a serious flaw of the Weinberg-Salam theory. A possible scheme without such fields is described. The symmetry breaking is induced by a new strongly interacting sector whose natural scale is of the order of a few TeV.

### ACKNOWLEDGMENT

I would like to thank K. Wilson for explaining the reasons why scalar fields require unnatural adjustments of bare constants.

UNIFIED GAUGE THEORIES  
WITHOUT ELEMENTARY SCALAR FIELDS

A thesis presented

by

John Phillip Preskill

to

The Department of Physics  
in partial fulfillment of the requirements  
for the degree of  
Doctor of Philosophy  
in the subject of  
Physics

Harvard University  
Cambridge, Massachusetts

May, 1980



Yet by the summer of 1980, Lenny, his T-shirt still soaked from a just-completed jog, stood in my office at Harvard loudly insisting that his earlier ideas about technicolor were deeply flawed and should be rejected. I resisted for many months before concluding that Susskind was probably right about having been wrong. It was an unforgettable lesson in scientific integrity.



# “Quantum Aspects of Black Holes”

Aspen Workshop

August 3 to September 4, 1992

Among the participants:

Tom Banks, Sidney Coleman, Steve Giddings, Stephen Hawking,

Gary Horowitz, Don Page, Malcolm Perry, John Preskill,

Andy Strominger, Lenny Susskind, Kip Thorne, Erik and Herman Verlinde

4. Susskind - "The Puzzle of BH Evaporation" 14 Aug. 92

Little learned about  $g$  grav and  $q$  em  
 - No guidance from exp  
 - No remote

History - Gedanken exp  
 o Mismatch of Newton + Maxwell - Einstein running along light ray

Not special line  
 [ o Thermo + equipartition of radiation  
 o Elevator in case of GR

Now [  $\Lambda = 0$   
 Black Holes ] maybe not for 20 yrs  
 Glimpse of the next revolution

Monsters - viol of B laws  
 3 AS - viol of QM itself !!

Heroes - Bekenstein  
 Hawking

History: Beginning: Area Theorem  
 Bekenstein: Generalized 2nd Law

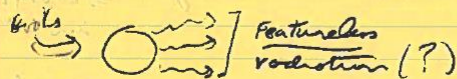
Can't # of ways to make BH  $\bigcirc r = M$

Use photons with  $h\nu$

$$\frac{M}{\omega} \sim r^2 \quad dE = T dS \Rightarrow T \sim \frac{1}{M}$$

$$\Rightarrow L \sim \frac{1}{M^2} \Rightarrow E \sim M^3$$

H/dim models confirm this picture in back reaction calc



S-matrix?  
 orthogonal initial  $\Rightarrow$   
 orthogonal final

Real honest dilemma

Another way out?



horizon is nice place  
 sing is terrible (we don't know what happens)  
 can info propagate along his spacelike curve  
 then finally comes out

but only  $\sim M$  left for greyhole of info  
 $\Rightarrow$  info takes a very long time to come out (stretch radiation)  
 $\Rightarrow$  "stable remnant"

solutions:

Go beyond semiclassical fluctuations in sing and horizon

no superseded self (from string theory)

no no of conserved quantities  $\Rightarrow$  Krivov S-matrix

Info lost: Can't stop there... becomes compulsory  
 Sym + Cons laws no longer conserved  
 $\Rightarrow$  energy not conserved  
 cf - noise quenched randomness  
 heats a system up

What small parameter makes info less small? Energy density?  
 put energy of view at black hole  
 $\Rightarrow$  0(1) violation of energy at this side

Stable Remnants: Carry the info  $\Rightarrow$  enormous level density near black side  
 Dangerous in QFT - eq. enormous from a big BH

- Hawking - info lost
- tHooft - unitary S-matrix for profound reasons
- Polchinski - info lost. No way to retrieve it
- Strominger - remnant
- Coleman - dump of coal
- Wilczek - Technical problem - still open here at school
- Witten - Problem not interesting



- Hawking - info lost
- 't Hooft - unitary S matrix for profound reasons
- Polchinski - info lost. No way to retrieve it
- Strominger - remnant
- Coleman - dump of cool
- Wilczek - Technical problem - I'll soon have it solved
- Witten - Problem not interesting

There is an emerging consensus among the participants that Hawking is essentially right—that the information loss paradox portends a true revolution in fundamental physics. If so, then one must go further, and develop a sensible “phenomenological” theory of information loss. One must reconcile the fact of information loss with established principles of physics, such as locality and energy conservation. We expect that many people, stimulated by their participation in the workshop, will now focus attention on this challenge.

John Preskill and Andy Strominger

## **Do Black Holes Destroy Information?\***

John Preskill

*California Institute of Technology, Pasadena, CA 91125*

I review the information loss paradox that was first formulated by Hawking, and discuss possible ways of resolving it. All proposed solutions have serious drawbacks. I conclude that the information loss paradox may well presage a revolution in fundamental physics.

# **DIFFICULTIES FOR THE EVOLUTION OF PURE STATES INTO MIXED STATES**

Thomas BANKS\* and Leonard SUSSKIND\*\*

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Michael E. PESKIN†

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Received 5 January 1984

Motivated by Hawking's proposal that the quantum-mechanical density matrix  $\rho$  obeys an equation more general than the Schrödinger equation, we study the general properties of evolution equations for  $\rho$ . We argue that any more general equation for  $\rho$  violates either locality or energy-momentum conservation.

# “Quantum Aspects of Black Holes”

ITP Conference, UCSB

June 21-25, 1993

Among the participants:

Gary Gibbons, Gerard 't Hooft, Joe Polchinski, John Preskill,  
Lenny Susskind, Kip Thorne, Herman Verlinde, Bob Wald, ...



## Polchinski's Poll

1. Information is lost (unitarity violated)
2. Information escapes (causality violated)
3. Planck-scale black hole remnants
4. None of the above.

The vote favored “escape” over “loss” by a 60-40 margin.

The audience was 60% HEP theorists, 40% GR.

LS: Why is this meeting so much better than the one you organized last year?

JP: Because now you think you know the answer.

## The stretched horizon and black hole complementarity

Leonard Susskind,\* L arus Thorlacius,<sup>†</sup> and John Uglum<sup>‡</sup>

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(Received 21 June 1993)

Three postulates asserting the validity of conventional quantum theory, semiclassical general relativity, and the statistical basis for thermodynamics are introduced as a foundation for the study of black-hole evolution. We explain how these postulates may be implemented in a “stretched horizon” or membrane description of the black hole, appropriate to a distant observer. The technical analysis is illustrated in the simplified context of  $(1+1)$ -dimensional dilaton gravity. Our postulates imply that the dissipative properties of the stretched horizon arise from a coarse graining of microphysical degrees of freedom that the horizon must possess. A principle of black-hole complementarity is advocated. The overall viewpoint is similar to that pioneered by ’t Hooft but the detailed implementation is different.

## Gedanken experiments involving black holes

Leonard Susskind\* and L arus Thorlacius<sup>†</sup>

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(Received 25 August 1993)

Analysis of several gedanken experiments indicates that black hole complementarity cannot be ruled out on the basis of known physical principles. Experiments designed by outside observers to disprove the existence of a quantum-mechanical stretched horizon require knowledge of Planck-scale effects for their analysis. Observers who fall through the event horizon after sampling the Hawking radiation cannot discover duplicate information inside the black hole before hitting the singularity. Experiments by outside observers to detect baryon number violation will yield significant effects well outside the stretched horizon.

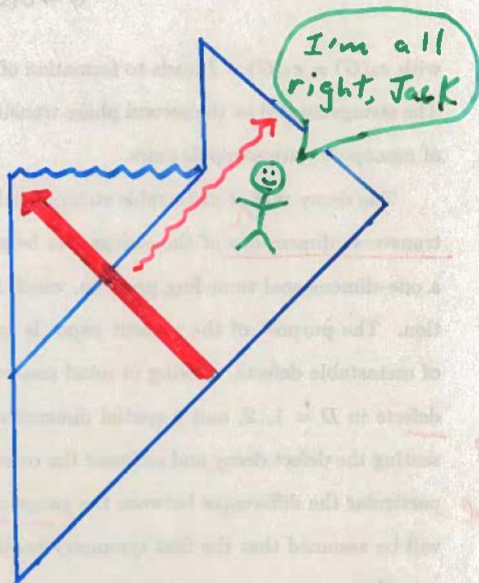
In many respects, the situation seems comparable to that of the early part of the century. The contradictions between the wave and particle theories of light seemed irreconcilable, but careful thought could not reveal any logical contradiction. Experiments of one kind or the other revealed either particle or wave behavior, but not both. We suspect that the present situation is similar. **An experiment of one kind will detect a quantum membrane, while an experiment of another kind will not. However, no possibility exists for any observer to know the results of both.** Information involving the results of these two kinds of experiments should be viewed as *complementary* in the sense of Bohr.

In this paper we shall illustrate the concept of black hole complementarity by considering a number of gedanken experiments where one might expect contradictions to arise. The basic argument we apply was formulated most clearly by Preskill [3]. It says that **apparent contradictions can always be traced to unsubstantiated assumptions about physics at or beyond the Planck scale.**

Hoofit / Susskind Credo:

It is all right to do bad things,  
as long as no one can ever  
find out!

"Causality  
violation"  
that no  
conceivable  
observer can  
detect.

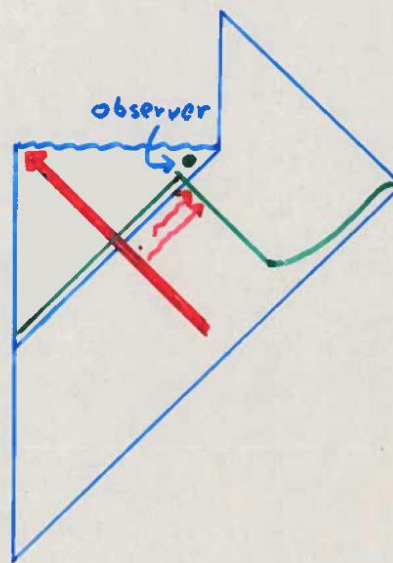


To the outside observer,  
information might as well have  
been destroyed at the global  
horizon, so it can be copied  
at the (stretched) horizon.

What about inside?

Observer behind global horizon  
has rights, too! Can he infer  
that information has escaped from  
behind the horizon?

Assume black hole S-Matrix is known:



- Highly blue-shifted message?
- Horizon fluctuations?

# “Geometry and Gravity”

Newton Institute, Cambridge

June 1-30, 1994

Among the participants:

Gary Gibbons, Jeff Harvey, Stephen Hawking, John Preskill,  
Rafael Sorkin, Andy Strominger, Lenny Susskind, Herman Verlinde, ...



# The World as a Hologram

LEONARD SUSSKIND

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## ABSTRACT

According to 't Hooft the combination of quantum mechanics and gravity requires the three dimensional world to be an image of data that can be stored on a two dimensional projection much like a holographic image.

The two dimensional description only requires one discrete degree of freedom per Planck area and yet it is rich enough to describe all three dimensional phenomena. After outlining 't Hooft's proposal I give a preliminary informal description of how it may be implemented. One finds a basic requirement that particles must grow in size as their momenta are increased far above the Planck scale. The consequences for high energy particle collisions are described.

The phenomena of particle growth with momentum was previously discussed in the context of string theory and was related to information spreading near black hole horizons. The considerations of this paper indicate that the effect is much more rapid at all but the earliest times. In fact the rate of spreading is found to saturate the bound from causality. Finally we consider string theory as a possible realization of 't Hooft's idea. The light front lattice string model of Klebanov and Susskind is reviewed and its similarities with the holographic theory are demonstrated. The agreement between the two requires unproven but plausible assumptions about the nonperturbative behavior of string theory. Very similar ideas to those in this paper have long been held by Charles Thorn.

## Acknowledgements:

During the month of July of this year I visited Gerard 't Hooft in Utrecht. Much of my thinking about these problems was stimulated by our discussions during this time. The idea that the world is in a sense two dimensional is 't Hooft's but it resonated very closely with my own thinking about horizons and strings. The way of implementing the idea, and its possible connections with string theory, is mine but it was very heavily influenced by our conversations.

I would like to thank both 't Hooft and John Preskill for emphasizing that information can and should spread at the causal limit as matter approaches a horizon.



## Fast scramblers

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ABSTRACT: We consider the problem of how fast a quantum system can scramble (thermalize) information, given that the interactions are between bounded clusters of degrees of freedom; pairwise interactions would be an example. Based on previous work, we conjecture:

- 1) The most rapid scramblers take a time logarithmic in the number of degrees of freedom.
- 2) Matrix quantum mechanics (systems whose degrees of freedom are  $n$  by  $n$  matrices) saturate the bound.
- 3) Black holes are the fastest scramblers in nature.

The conjectures are based on two sources, one from quantum information theory, and the other from the study of black holes in String Theory.

### Acknowledgments

This paper was inspired by conversations with Patrick Hayden. We are very grateful to him for explaining the subtleties of quantum information theory that went into [4]. We are also indebted to Steve Shenker, Joe Polchinski, Debbie Leung, Daniel Gottesman, and John Preskill for helpful insights and comments.

## Cool horizons for entangled black holes

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General relativity contains solutions in which two distant black holes are connected through the interior via a wormhole, or Einstein-Rosen bridge. These solutions can be interpreted as maximally entangled states of two black holes that form a complex EPR pair. We suggest that similar bridges might be present for more general entangled states.

In the case of entangled black holes one can formulate versions of the AMPS(S) paradoxes and resolve them. This suggests possible resolutions of the firewall paradoxes for more general situations.

“The ER = EPR conjecture seems to allow us to view the early radiation with which the black hole is entangled as a complementary description of the black hole interior.”

“Entanglement = Wormholes,” Quantum Frontiers, 7 June 2013

## Holographic Complexity Equals Bulk Action?

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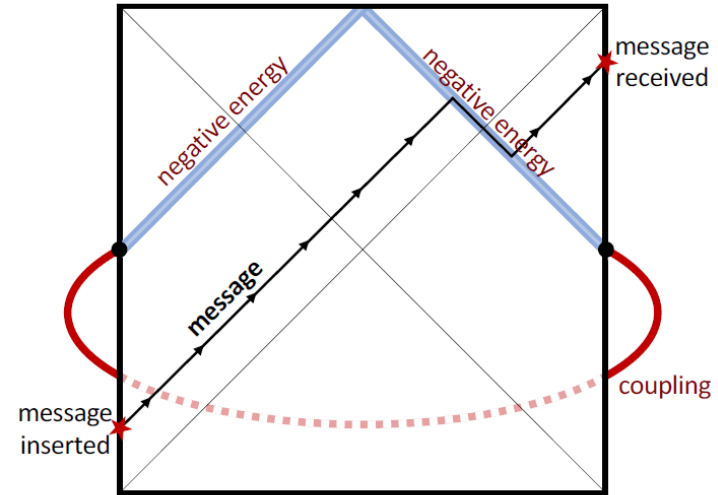
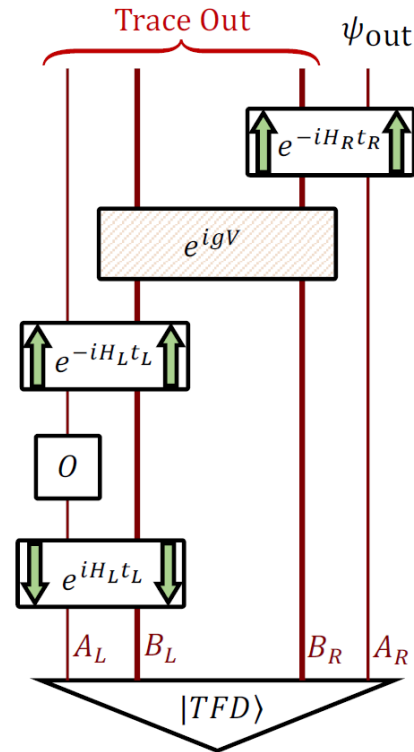
<sup>2</sup>*Center for Theoretical Physics and Department of Physics, Massachusetts Institute of Technology,  
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We conjecture that the quantum complexity of a holographic state is dual to the action of a certain spacetime region that we call a Wheeler-DeWitt patch. We illustrate and test the conjecture in the context of neutral, charged, and rotating black holes in anti-de Sitter spacetime, as well as black holes perturbed with static shells and with shock waves. This conjecture evolved from a previous conjecture that complexity is dual to spatial volume, but appears to be a major improvement over the original. In light of our results, we discuss the hypothesis that black holes are the fastest computers in nature.

# Quantum gravity in the lab

Brown, Gharibyan, Leichenauer, Lin, Nezami, Salton, Susskind, Swingle, Walter 1911.06314



Use gravitational intuition to understand complex emergent quantum phenomena?

Measure features of quantum gravity that are hard to analyze classically?

What quantum systems have useful gravitational duals?





John Prichard

Leonard



**From JP to LS, 26 Oct 2001**

One of my co-authors is Alexei Kitaev, and he is one of the most brilliant guys I've known. A week or two ago, he went to UCLA to hear your talk, as he's very interested in the quantum Hall effect.

The next day we had this conversation:

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AK: I heard a talk about how string theory explains the quantum Hall effect, but I did not understand anything.

JP: Who gave the talk?

AK: I don't know. Someone from Stanford. (AK is one of these Russians who is not interested in who people are ...)

JP: Was it Lenny Susskind? He's my favorite physicist!

AK: I don't know. I will have to look at the program.

JP: Well, was he an old guy with a beard?

AK: No. He had a beard, but he was not old.

=====

And of course he's right. You're not.